$\qquad$ Exam Seat No: $\qquad$

## C.U. SHAH UNIVERSITY

## Summer Examination-2020

## Subject Name: Mathematics

Subject Code: 4CS01IMT1
Semester: 1
Date:02/03/2020
Branch: B.Sc.I.T.
Time: 02:30 to 05:30
Marks: 70

## Instructions:

(1) Use of Programmable calculator \& any other electronic instrument is prohibited.
(2) Instructions written on main answer book are strictly to be obeyed.
(3) Draw neat diagrams and figures (if necessary) at right places.
(4) Assume suitable data if needed.

## Q-1 Attempt the following questions:

a) If two sets $A$ and $B$ then $A$ union $B$ is denoted by $\qquad$ .
a) $A \cap B$
b) $A \cup B$
c) $A \subset B$
d) $A \supset B$
b) If $A=\{2,4,5,7\}$ then $\qquad$ elements in $P(A)$.
a) 14
b) 16
c) 15
d) 17
c) If $A=\left[\begin{array}{ll}1 & 0\end{array}\right]$ and $B=\left[\begin{array}{l}1 \\ 0\end{array}\right]$ then $A B=$ $\qquad$ .
a) $\left[\begin{array}{ll}1 & 1\end{array}\right]$
b) $\left[\begin{array}{ll}0 & 0\end{array}\right]$
c) $[0]$
d) $[1]$
d) If $A=\left[\begin{array}{ll}2 & 1 \\ 0 & 4\end{array}\right]$ and $B=\left[\begin{array}{cc}1 & 0 \\ -3 & -4\end{array}\right]$ then $A-B$ $\qquad$ .
a) $\left[\begin{array}{ll}1 & 1 \\ 8 & 3\end{array}\right]$
b) $\left[\begin{array}{cc}1 & 1 \\ -3 & 8\end{array}\right]$
c) $\left[\begin{array}{cc}1 & -1 \\ 3 & 8\end{array}\right]$
d) $\left[\begin{array}{ll}1 & 1 \\ 3 & 8\end{array}\right]$
e) If $A=A^{T}$ then $A$ is $\qquad$ .
a) skew symmetric
b) symmetric
c) Lower Triangular
d) none of these
f) Complete the series $0,3,8,15$,?
a) 23
b) 24
c) 25
d) 22
g) $20 \%$ of 4000 are $\qquad$ .
a) 850
b) 600
c) 800
d) 80
h) In a certain code, INDIA is written as JOEJB, how is GERMANY written in that code?
a)HFSNBOZb) HDSNBMZ
c) HFRNBOZd) HFSNAOZ
i) Complete the series $7,10,8,11,9,12$,?
a) 11
b) 13
c) 12
d) 10
j) $\frac{d}{d x}\left(e^{2 x}\right)=$ $\qquad$ .
a) $e^{2 x}$
b) $2 e^{2 x}$
c) $\frac{e^{2 x}}{2}$
d) none of these
k) $\frac{d}{d x}\left(a^{x}\right)=$ $\qquad$ .
a) $a^{x}$ b) 1
c) 0
d) $a^{x} \log a$

1) $\int \sin x d x=$ $\qquad$ $+\mathrm{c}$.
a) $\cos x$
b) $\sin x$
c) $-\cos x$
d) $-\sin x$
m) $\int 1 d x=$ $\qquad$ +c .
a) $x$
b) 1
c) 0
d) none of these
n) $\frac{d}{d x}(\log x)=$ $\qquad$ .
a) $x \log x$
b) $x+\log x$
c) $1+\log x$
d) $\frac{1}{x}$

## Attempt any four questions from $\mathbf{Q}-2$ to $\mathbf{Q - 8}$

## Q-2 Attempt all questions

a) If $A=\{1,2,3,4,5\}, B=\{2,4,6,8\}, C=\{x \mid x \in N, x$ is multipale of $3, x<10\}$ then prove that $(A \cup B) \cup C=A \cup(B \cup C)$.
b) If $U=\{-1,0,1,2,3,4,5\}$ be universal set and $A=\{-1,0,1\}$ is a given set. Then verify
(i) $A \cup A^{\prime}=U$
(ii) $A \cap A^{\prime}=\varnothing$
$\left(\right.$ iii) $\left(A^{\prime}\right)^{\prime}=A$
c) Find the number of subsets of set $A=\{1,2,3\}$. Also find power set of $A$.

## Q-3 Attempt all questions

a) If $A=\left[\begin{array}{ccc}4 & 8 & 1 \\ -2 & -2 & -1 \\ 6 & -4 & 2\end{array}\right]$ and $B=\left[\begin{array}{ccc}8 & 4 & 0 \\ 6 & -2 & 8 \\ 4 & -1 & -6\end{array}\right]$ then find $A B$.
b) If $A=\left[\begin{array}{ll}2 & 3 \\ 1 & 4\end{array}\right]$ and $B=\left[\begin{array}{ll}5 & 1 \\ 0 & 3\end{array}\right]$ are two matrices then verify that $(A B)^{T}=B^{T} A^{T}$.
c) If $A=\left[\begin{array}{ccc}1 & 2 & 3 \\ 1 & 3 & 5 \\ 1 & 5 & 12\end{array}\right]$ then find $\operatorname{adj}(A)$.

## Q-4 Attempt all questions

a) Find the inverse of the matrix $A=\left[\begin{array}{lll}1 & 1 & 2 \\ 1 & 9 & 3 \\ 1 & 4 & 2\end{array}\right]$.
b) Complete the following series.

1) $21,9,21,11,21,13,21$, $\qquad$
2) $58,52,46,40,34$, $\qquad$
3) $3,4,7,8,11,12$, $\qquad$
4) $2,4,9,16,25,36$, $\qquad$
c) The circle-graph given here shows the spending of a country on various sports during a particular year. Study the graph carefully and answer the questions given below it.

5) What percent of total spending is spent on Tennis?
6) If the total amount spent on sports during the year be Rs. $1,80,00,000$, the amount spent on Basketball exceeds on Tennis by $\qquad$

## Q-5 Attempt all questions

1) In a mixture 60 litres, the ratio of milk and water $2: 1$. If this ratio is to be $1: 2$, then
a) the quantity of water to be further added is $\qquad$ .
2) If $0.75: x:: 5: 8$, then $x$ is equal to $\qquad$ .
b) There is $60 \%$ increase in an amount in 6 years at simple interest. What will be the compound interest of Rs. 12,000 after 3 years at the same rate?
c) Two students appeared at an examination. One of them secured 9 marks more than the other and his marks was $56 \%$ of the sum of their marks. What were the marks obtained by them?

## Q-6 Attempt all questions

a) 1) The percentage profit earned by selling an article for Rs. 1920 is equal to the percentage loss incurred by selling the same article for Rs. 1280. At what price should the article be sold to make $25 \%$ profit?
2) When a plot is sold for Rs. 18,700 , the owner loses $15 \%$. At what price must that plot be sold in order to gain $15 \%$ ?

b) Study the following table and answer the questions.

Number of Candidates Appeared and Qualified in a Competitive Examination from Different States Over the Years.

| STATE | Years |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1997 |  | 1998 |  | 1999 |  | 2000 |  | 2001 |  |  |  |  |  |  |  |
|  | App. | Qual. | App. | Qual. | App. | Qual. | App. | Qual. | App. | Qual. |  |  |  |  |  |  |
| M | 5200 | 720 | 8500 | 980 | 7400 | 850 | 6800 | 775 | 9500 | 1125 |  |  |  |  |  |  |
| N | 7500 | 840 | 9200 | 1050 | 8450 | 920 | 9200 | 980 | 8800 | 1020 |  |  |  |  |  |  |
| O | 6400 | 780 | 8800 | 1020 | 7800 | 890 | 8750 | 1010 | 9750 | 1250 |  |  |  |  |  |  |
| P | 8100 | 950 | 9500 | 1240 | 8700 | 980 | 9700 | 1200 | 8950 | 995 |  |  |  |  |  |  |
| R | 7600 | 870 | 7600 | 940 | 9800 | 1350 | 7600 | 945 | 7950 | 885 |  |  |  |  |  |  |

1) Total number of candidates qualified from all the states together in 1997 is approximately what percentage of the total number of candidates qualified from all the states together in 1998 ?
2) What is the average candidates who appeared from State $Q$ during the given years?
3) The percentage of total number of qualified candidates to the total number of appeared candidates among all the five states in 1999 is?
c) In certain coding system fill the blank.
4) $\mathrm{CMM}, \mathrm{EOO}, \mathrm{GQQ}$, $\qquad$ , KUU
5) FAG, GAF, HAI, IAH, $\qquad$ , MLNA
6) ELFA, GLHA, ILJA, $\qquad$
7) SCD, TEF, UGH, $\qquad$ WKL

## Q-7 Attempt all questions

a) Evaluate $\int x^{2} \sin x d x$ by method of integration by parts.
b) Find: $\frac{d}{d x}\left(\frac{x \cos x}{1+x^{2}}\right)$
c) Find: $\int\left(5 x^{4}+3 x^{2}+\sin 2 x\right) d x$

## Q-8 Attempt all questions

a) Find the differentiation of $\frac{e^{x}\left(x^{2}+2\right)}{x^{3}}$ w.r.t. $x$.
b) If $x=a t^{2} \& y=2 a t$ then find $\frac{d y}{d x}$.
c) Find: $\int \frac{(1+\log x)^{2}}{x} d x$

